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Massachusetts Institute of Technology, 77 Massachusetts Ave, Cambridge, MA 02139. *Decidable
Prime Models*. Preliminary report.

A set S of types over a theory T is **strongly free** if for all subsets $X \subset S$, there is a countable model of T which realizes X and omits $S \setminus X$. Throughout, all theories are assumed complete and consistent. **Theorem** *If all strongly free sets of types over a computable theory T are finite, then T has a decidable prime model.* A classical result in model theory is that any theory with less than 2^{\aleph_0} many countable models must have a prime model. Our theorem gives an effective extension of this result: **Corollary** *If a countable theory T has less than 2^{\aleph_0} many countable models, then there is a prime model of T computable in T .* The Barwise Compactness theorem lies at the heart of the proof, giving rise to a result in classical recursion theory with a higher recursion theoretic proof. (Received September 30, 2000)