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A graph  $G$  is *k-dot-critical* if it has domination number  $k$  and identifying any two adjacent vertices results in a graph with domination number  $k - 1$ . A graph  $G$  is *totally useable* if every vertex of  $G$  lies in some minimum dominating set. A graph  $G$  is *critically dominated* if the set of critical vertices forms a dominating set. We present a number of characteristics of graphs having these properties, and in particular we provide a constructive characterization of dot-critical trees and show that for trees, the properties dot-critical, totally useable and critically dominated are the same. (Received October 02, 2000)