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We will present an equivalent formulation of the special case of Knesser's theorem on the densities of sequences. We then use this formulation to prove a theorem that for the purposes of zero-sum applications, shows in many cases that it is actually easier to find zero-sum solutions when the Cauchy-Davenport theorem does not apply (for general  $m$ ). Finally we use this theorem to show that the four color Rado number for the following problem, first introduced by Erdős, zero-sum generalizes: For positive integers  $m$  and  $r$ , let  $f(m, \mathbb{Z}_m^{(k)})$  be the minimum integer such that for every coloring of the integers  $[1, f(m, \mathbb{Z}_m^{(k)})]$  by the elements of  $k$  disjoint labeled copies of  $\mathbb{Z}_m$ ,  $\mathbb{Z}_m^{(k)} = \mathbb{Z}_m^1 \cup \mathbb{Z}_m^2 \cup \dots \cup \mathbb{Z}_m^k$ , there exist two zero-sum subsets  $B_1, B_2 \subseteq [1, f(m, \mathbb{Z}_m^{(k)})]$ , which satisfy: (i)  $|B_1| = |B_2| = m$ ; (ii) the greatest integer in  $B_1$  is less than the least integer in  $B_2$ ; (iii) the diameter of the convex hull spanned by  $B_1$  does not exceed the diameter of the convex hull spanned by  $B_2$ . We are able to determine that  $f(m, \mathbb{Z}_m^2) = 12m - 9$ . (Received October 03, 2000)