

962-05-212

**Joshua E Greene\*** (jgreene@hmc.edu), 7123 Smooth Path, Columbia, MD 21045. *Chromatic Capacities of Graphs and Hypergraphs.*

Given a hypergraph  $H$ , the *chromatic capacity*  $\chi_{cap}(H)$  of  $H$  is the largest  $k$  for which there exists a  $k$ -coloring of the edges of  $H$  such that, for every coloring of the vertices of  $H$  with the edge colors, there exists an edge that has the same color as both of its endpoints. When  $H$  is an  $r$ -regular hypergraph,  $r > 1$ , with maximum degree  $\Delta$ , we show that  $\chi_{cap}(H) < (1 + o(1))\sqrt[r]{r\Delta}$ , improving a result of Cochand and Károlyi (Discrete Math. 194 (1999) 249-252). This in turn yields an improved bound of  $\hat{\chi}^{(k)}(\mathbb{R}) < (4 + o(1))k$ , where  $\hat{\chi}^{(k)}(\mathbb{R})$  denotes the  $k$ th upper chromatic number of the reals. We also answer a question of Archer (Discrete Math. 214 (2000) 65-75) by exhibiting a family of graphs for which  $\chi_{cap}(G) = \chi(G) - 1$  for arbitrarily large  $\chi(G)$ , the ordinary chromatic number of the graph  $G$ . Lastly, we give a complete characterization of graphs  $G$  with  $\chi_{cap}(G) = 1$ . (Received August 28, 2000)