

962-05-635

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The Petersen block P is the cocycle matroid of the Petersen graph. It is a 15-point rank-6 binary simple matroid. It is the only known tangential block which “splits” into the union of two proper flats which is not a q -cone (or a q -lift). All other known splitting tangential blocks are q -cones of P . In this talk, we describe this splitting. The Petersen block is the union of two copoints or rank-5 flats. Both copoints are isomorphic to the cycle matroid $M(W_5)$ of the 5-wheel. They intersect at a rank-4 flat which is a 5-circuit. Thus, P can be obtained by taking the union of two $M(W_5)$ ’s and “suitably” identifying the points in the rim of the two wheels. This description of the Petersen block leads to the following conjecture, which forms a small part of the Tutte tangential 2-block conjecture: the Petersen block is the only splitting binary tangential 2-block with rank greater than 4 in which every point is on at least two 3-point lines. (Received September 18, 2000)