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**Derek A Smith\*** ([smithder@lafayette.edu](mailto:smithder@lafayette.edu)), Math Department, Lafayette College, Easton, PA 18042. *Four-generator partial Boolean algebras in orthomodular lattices.*

In orthodox quantum mechanics, the properties of a quantum mechanical system correspond to the closed subspaces of a Hilbert space. Two properties are said to be compatible if their associated subspaces are orthogonal outside of any intersection. The set of subspaces generated from an initial set  $S$  under the operations of orthogonal complement and intersection of compatible subspaces is a partial Boolean algebra  $B(S)$  as introduced by Kochen and Specker. Conway and Kochen have exhibited a set  $T$  of five subspaces in  $\mathbb{C}^4$  that generate an infinite  $B(T)$ . Here, we show that  $T$  has a minimal number of generators by proving that every set  $S$  of four elements in any orthomodular lattice of height four generates a finite  $B(S)$ . (Received October 03, 2000)