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Mugurel A. Barcau* (barcau@math.unm.edu), University of New Mexico, Department of Mathematics and Statistics, Albuquerque, NM 87131. *The affine line modulo isogeny.*

Let $Y(1)$ classify the isomorphism classes of elliptic curves E/\mathbf{C} . Then one has an analytic isomorphism $j : Y(1) \longrightarrow \mathbb{A}_{\mathbf{C}}^1$, $E \longmapsto j(E)$ onto the set of \mathbf{C} -points of the affine line, where $j(E)$ is the j -invariant of the elliptic curve E/\mathbf{C} . We say that $x \in \mathbb{A}_{\mathbf{C}}^1$ is isogeneous to $y \in \mathbb{A}_{\mathbf{C}}^1$, in notation $x \overset{isog}{\sim} y$, if there exists an isogeny $\pi : E_x \longrightarrow E_y$ defined over \mathbf{C} , with $x = j(E_x)$ and $y = j(E_y)$. Let $\mathbb{A}_{\mathbf{C}}^1/isogeny$ be the set of cosets of $\mathbb{A}_{\mathbf{C}}^1$ modulo the equivalence relation $\overset{isog}{\sim}$. We cannot expect to find any reasonable object in the usual algebraic geometry, whose \mathbf{C} -points are naturally in bijection with $\mathbb{A}_{\mathbf{C}}^1/isogeny$, because the equivalence classes of $\overset{isog}{\sim}$ are dense in the complex topology. We will be able to find a geometric substitute for the quotient “ $\mathbb{A}^1/isogeny$ ” in the “new” geometry obtained by “adjoining” one new operation to the “classical” one, that plays the role of a derivation. (Received October 03, 2000)