

962-11-1235

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We report on various relations between theta functions and torsion points on certain algebraic groups. In particular, we consider modular forms  $f_n$  which are products of derivatives at 0 of theta functions with rational characteristics of order  $n$ , and show that  $f_n$  vanishes at the period matrix  $\tau$  of an elliptic curve  $E$  precisely when  $E$  has a special point of order  $n$  we call a “singular” torsion point. The singular torsion points on  $E$  are related to torsion points on the image of  $E$  embedded in a certain generalized Jacobian, and from a result of Hindry we find that only finitely-many of the  $f_n$  vanish for any given  $\tau$ . When  $E$  is defined over a number field, we describe a procedure which in principle can determine all the singular torsion on  $E$ . (Received October 02, 2000)