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John M. Holte* (holte@gac.edu), Department of Mathematics & Computer Science, Gustavus Adolphus College, 800 W. College Ave., St. Peter, MN 56082. *Fractal Dimension of Generalized Multinomial Coefficients Modulo a Prime*. Preliminary report.

Given a sequence (u_n) of positive integers generated by $u_1 = 1, u_2 = a, u_n = au_{n-1} + bu_{n-2} (n \geq 3)$, define the generalized factorial by $[n]! = u_1 u_2 \cdots u_n$ and the generalized d -nomial coefficient by $C(n_1, \dots, n_d) = [n_1 + \cdots + n_d]! / ([n_1]! \cdots [n_d]!)$.

Assume that the prime p does not divide b . Let $r = \min\{n : p|u_n\}$. **Theorem 1 (Asymptotic abundance of residues):** $\#\{(n_1, \dots, n_d) | 0 \leq n_1, \dots, n_d < rp^k \text{ and } C(n_1, \dots, n_d) \equiv \rho \pmod{p}\} \sim \frac{1}{p-1} \binom{r+d-1}{d} \binom{p+d-1}{d}^k$ as $k \rightarrow \infty$ for $\rho = 1, \dots, p-1$.

Theorem 2 (Fractal dimension): Let $s_k = rp^k$.

The Hausdorff dimension of $\bigcap_k \cup \{[n_1/s_k, (n_1+1)/s_k) \times \cdots \times [n_d/s_k, (n_d+1)/s_k) | 0 \leq n_1, \dots, n_d < s_k, p \nmid C(n_1, \dots, n_d)\}$ is $\log \binom{p+d-1}{d} / \log p$. (Received September 28, 2000)