

962-13-1200

Daniel D. Anderson (dan-anderson@uiowa.edu), Iowa City, IA 52242, and **Sylvia J Forman*** (syforman@sju.edu), Philadelphia, PA 19131. *Two star-operations and their induced lattices.*
Preliminary report.

Let D be an integral domain with quotient field K , let $F(D)$ ($f(D)$) be the set of nonzero (finitely generated) fractional ideals of D , and let \star be a star-operation on $F(D)$. For $A \in F(D)$ we will define $A^{\bar{\star}} = \{x \in K \mid \text{there exists a } J \in F(D) \text{ such that } J^{\star} = D \text{ and } xJ \subseteq A\}$ and $A^{\star_w} = \{x \in K \mid \text{there exists a } J \in f(D) \text{ such that } J^{\star} = D \text{ and } xJ \subseteq A\}$. Then $\bar{\star}$ and \star_w are star-operations on $F(D)$ that satisfy $(A \cap B)^{\bar{\star}} = A^{\bar{\star}} \cap B^{\bar{\star}}$ and $(A \cap B)^{\star_w} = A^{\star_w} \cap B^{\star_w}$. Let $\mathcal{L}_{\star}(D) = \{A \mid A \text{ is an integral } \star\text{-ideal}\} \cup \{0\}$. Then $\mathcal{L}_{\star}(D)$ is a complete multiplicative lattice which is modular if \star distributes over intersections. If we call a star-operation modular when its induced lattice is modular, then for a finite character star-operation \star on $F(D)$, it is of interest to know the exact relationship between the following three conditions: (1) \star is additive, (2) \star distributes over intersections, and (3) $\mathcal{L}_{\star}(D)$ is modular. (Received October 03, 2000)