

962-13-32

**David E Dobbs\*** (dobbs@math.utk.edu), Department of Mathematics, University of Tennessee, Knoxville, TN 37996-1300, and **Bernadette Mullins**, Department of Mathematics, Birmingham Southern College, Arkadelphia Road Box 549001, Birmingham, AL 35254. *On the lengths of maximal chains of intermediate fields in a field extension.*

We study two invariants,  $\nu(L/K)$  and  $\lambda(L/K)$ , arising from a field extension  $L/K$ . These are, respectively, the cardinal number of the set of fields contained between  $K$  and  $L$ ; and the supremum of the set of cardinal numbers arising as lengths of chains of such fields. We next state three typical results. If  $L$  can be generated by one element over an infinite field  $K$  and  $2 \leq [L : K] = n < \infty$ , then  $\nu(L/K) \leq 2^{n-2} + 1$ , with equality if  $L/K$  is Galois with the Klein four-group as Galois group. For each infinite cardinal number  $\aleph$ , there exists a field  $K$  such that if  $L$  denotes an algebraic closure of  $K$ , then  $\lambda(L/K) = 2^\aleph = \nu(L/K)$ . If  $L/K$  is any nonalgebraic finitely generated field extension, then  $\lambda(L/K) = \aleph_0$ . (Received June 26, 2000)