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Maria A. Avino-Diaz* (mavino@campus.ccm.itesm.mx), Ave. Universidad 2014, Venezuela F-1203, Copilco, Coyoacan, 04510 Mexico City, Mexico, and Luis D. Garcia (galuis@nmsu.edu), Department of Mathematical Sciences, MSC 3MB, P.O. Box 30001, Las Cruces, NM 88003-8001. A p-Bases Algorithm for Indecomposable $\mathbf{Z}_{p^n}C_p$ -Modules.

Let \mathbf{Z}_{p^n} be the ring of integers modulo p^n , $n \geq 2$, and $C_p = \langle x : x^p = 1 \rangle$ the cyclic group of order a prime number p. Let $\Lambda = \mathbf{Z}_{p^n}C_p$ be the group algebra over \mathbf{Z}_{p^n} . The problem of describing the finite modules of this group algebra has been considered by Szekeres (1949) and Nazarova-Roiter (1969). In both papers a description of the indecomposable modules is given. Aviñó and Bautista calculated the \mathbf{Z}_{p^n} -structure of the indecomposable Λ -modules M without taking p-bases of the abelian p-group M. Instead of this modules are well studied, the matrices of $\phi = x - 1 \in \Lambda$ and $\pi = x^{p-1} + \cdots + x + 1 \in \Lambda$ are not known. In this work we introduce binomial ideals associated to finitely generated abelian groups, the descrition of reduced Gröbner bases of these ideals, and p-basis associated to the reduced Gröbner bases. We present algorithms which obtain a p-basis of the Λ -module M and the matrices of ϕ and π in this p-basis using the invariants of the Λ -module. (Received September 29, 2000)