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A projective variety X is called *projectively normal* if its homogeneous coordinate ring is integrally closed. More geometrically, this means that hypersurfaces of any degree $t \geq 1$, in the ambient projective space, cut on X complete linear systems. The hardest step in establishing the projective normality of a variety is usually the case $t = 2$. This question can be addressed by understanding how many quadric hypersurfaces contain the given variety. In this context, the present paper examines ruled surfaces in \mathbb{P}^5 which are contained in singular quadric hypersurfaces. A complete classification is given for ruled surfaces contained in quadrics of rank 5 and a series of general results are found in the cases of lower ranks. Part of the classification is achieved by first finding upper bounds for a list of numerical invariants and subsequently having Maple perform the remaining finite number of numerical checks. (Received August 08, 2000)