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Let G be a finite group and k a field of characteristic $p > 0$. A kG -module M is an endotrivial module if $\text{Hom}_k(M, M)$ is the direct sum of a trivial kG -module and a projective kG -module. Equivalence classes of endotrivial modules modulo projective direct summands form a group under tensor product. The torsion free part of the group is detected on restriction to elementary abelian subgroups of rank two. In earlier work we showed that for G a p -group the torsion endotrivial modules are detected on extraspecial and almost extraspecial subgroups. In addition we were able to eliminate some cases when the prime p is odd. For the case that $p = 2$, we can show that many of the low rank extraspecial and almostextra special groups have no nontrivial torsion endotrivial modules. It seems likely that the techniques can be generalized to give a complete answer in even characteristic case. (Received September 21, 2000)