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**Scott T. Chapman**, Trinity University, 715 Stadium Drive, San Antonio, TX 78212-7200, **Ulrich Krause** ([krause@math.uni-bremen.de](mailto:krause@math.uni-bremen.de)), Bremen, Germany, and **Eberhard Oeljeklaus\*** ([oe1@math.uni-bremen.de](mailto:oe1@math.uni-bremen.de)), University of Bremen, Department of Mathematics, D-28334 Bremen, Germany. *On Diophantine Monoids and Their Class Groups.*

In the following context a monoid  $S$  is understood to be a finitely generated subgroup of an (additively written) abelian group  $G$  with  $S \cap \{n \cdot y \mid n \in \mathbf{N}, y \in G \setminus S\} = \{0\} = S \cap (-S)$ , where  $\mathbf{N}$  denotes the set of non-negative integers. It is known that  $S$  is a Krull monoid with finitely many essential states. Analyzing these states we prove in a rather straightforward way that  $S$  has a representation as a Diophantine monoid of size  $(m, n)$ , i.e. there is a matrix  $A \in \mathbf{Z}^{m \times n}$  such that  $S$  is isomorphic to the monoid  $M_A := \mathbf{N}^n \cap \{x \in \mathbf{Z}^n \mid Ax = 0\}$ . There are always Diophantine representations of  $S$  of minimal size  $(\tilde{m}, \tilde{n})$  in the sense that  $\tilde{m}$  and  $\tilde{n}$  are both minimal. We show that  $\tilde{m}$  equals the rank of the divisor class group  $Cl(S)$  of  $S$  and that  $\tilde{n}$  is the sum of the number of essential states of  $S$  with the rank of the torsion group of  $Cl(S)$ . (Received September 26, 2000)