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We generalize a claim from M.Gromov's book "Hyperbolic Groups" that in a torsion-free word-hyperbolic group G any k -generated non-free subgroup contains an element of "short" conjugacy length, where the "shortness" constant depends only on k and G . More precisely, we prove the following: **Theorem** *Let G be a word-hyperbolic group (not necessarily torsion-free) with a finite generating set X such that the Cayley graph $\Gamma(G, X)$ is δ -hyperbolic. Then for any integer $k \geq 1$ there exists a constant $C = C(k, \delta) > 0$ with the following property. Let $M = (g_1, \dots, g_k)$ be a k -tuple of elements of G . Let H be the subgroup of G generated by M . Then either H is free on M and quasiconvex in G or M is Nielsen-equivalent to a k -tuple $M' = (f_1, \dots, f_k)$ where the element f_1 is conjugate in G to an element of length at most $C(k, \delta)$.* This shows that in a non-free k -generated subgroup the conjugacy length of the first generator in a generating k -tuple can be made small. Further generalizations of this statement will also be discussed. (Received September 28, 2000)