

962-30-756

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A function f is in the class V_{2p} iff $f(z) = e^{-az^{2p+2}}g(z)$ where $a \geq 0$ and g is a constant multiple of a real entire function of genus $\leq 2p + 1$ with only real zeros. The class U_{2p} is defined as follows: $U_0 = V_0$, $U_{2p} = V_{2p} - V_{2p-2}$. Functions in the class U_{2p}^* are represented as $g(z) = c(z)f(z)$ where $f \in U_{2p}$ and c is a real polynomial with no real zeros. Every real entire function g , of finite order with at most finitely many non-real zeros satisfies $g \in U_{2p}^*$ for a unique p . We show, for a subclass of $f \in U_{2p}$, necessary and sufficient conditions for f'' to have exactly $2p$ non-real zeros. For a subclass of U_{2p}^* we show that if f' has only real zeros, then f'' has exactly $2p$ non-real zeros. For $f \in U_{2p}^*$ we show that $2p$ is a lower bound for the number of non-real zeros of $f^{(k)}$ for $k \geq 2$. (Received September 25, 2000)