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**Patrick S. Caldwell\*** ([psc1@ra.msstate.edu](mailto:psc1@ra.msstate.edu)), Department of Mathematics and Statistics,  
Mississippi State University, P.O. Drawer MA, Mississippi State, MS 399762. *Positive Solutions for  
Classes of Multiparameter Boundary Value Problems.*

In the recent past, many results have been established on non-negative solutions to boundary value problems of the form

$$\begin{aligned} -u''(x) &= \mu f(u(x)), 0 < x < 1 \\ u(0) &= u(1) = 0 \end{aligned}$$

where  $\mu > 0$ . In this paper, we study classes of multiparameter problems of the form

$$\begin{aligned} -u''(x) &= \lambda g(u(x)) + \mu f(u(x)), 0 < x < 1 \\ u(0) &= u(1) = 0 \end{aligned}$$

where  $f(0) < 0$  and  $g(0) > 0$ . We will discuss existence, multiplicity, and nonexistence of solutions for ranges of  $\lambda$  and  $\mu$ . We prove our analytical results via a quadrature method. Our results apply, for example, to the case when  $f(u) = (u + 1)^{\frac{1}{3}} - 2$  and  $g(u) = u^3 + 1$ , for which we also provide the complete bifurcation diagrams via numerical methods. (Received September 28, 2000)