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problem and discrepancy theory.*

We measure the irregularities of distribution (discrepancy) of an  $n$  element set of  $k$  planes  $\mathcal{P}_n \subset R^d$  by rotated and translated copies of a fixed convex body  $K$ . The body  $K$  has the Pompeiu property, if the integral of a continuous function  $f$  on the  $n$  dimensional Euclidean space vanish on every congruent copy of  $K$  then  $f$  is zero. The longstanding Pompeiu problem states that only the ball does not have the Pompeiu property. Assuming that  $K$  has the so called Pompeiu property and  $d - k \geq 2$  we give a  $C \cdot n^{\frac{1}{2} - \frac{1}{2(d-k)}}$  lower estimation for the discrepancy of  $\mathcal{P}_n$ , which is strict, using recent results. Our main result connects discrepancy theory, the theory of Radon transforms, Fourier analysis and overdetermined Neumann problems via the Pompeiu property of the body  $K$ . We also discuss a new proof (originally given by T. Kobayashi) for the Pompeiu problem if  $K$  is close to a ball. (Received October 03, 2000)