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**Bruce R. Ebanks\*** ([ebanks@math.msstate.edu](mailto:ebanks@math.msstate.edu)), Department of Mathematics & Statistics, 410 Allen Hall, Mississippi State University, Mississippi State, MS 39762. *On Non-homogeneous Cauchy Difference Equations of a Special Type.*

A problem posed at the 37th International Symposium on Functional Equations in May 1999 concerns equations of the form  $Cf(x, y) = bf(R(x, y))$ , for given rational functions  $R$  and for  $b$  equal to 1 or  $-1$ , where  $C$  is the Cauchy difference operator defined by  $Cf(x, y) = f(x + y) - f(x) - f(y)$ . Here the unknown  $f$  is a real-valued function on the positive reals. The problem is to determine which rational functions  $R$  admit nontrivial solutions of the equation. The author generalized the problem to  $Cf(x, y) = g(R(x, y))$  for two unknown functions  $f$  and  $g$ . Sufficient conditions for the existence of nontrivial solutions have been found, and these conditions include most (if not all) known results on equations of this type for positive real  $x$  and  $y$ . (Received September 22, 2000)