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Michael J Arciero* (arciero@math.uri.edu), Department of Mathematics, University of Rhode Island, Kingston, RI 02881. *Asymptotic Behavior of Szegő Polynomials with Respect to a Weak-star Convergent Sequence of Measures on the Unit Circle.*

Let $\phi_n(\theta)$, $n = 1, 2, 3, \dots$, be an approximate identity for $\mathcal{L}_1[-\pi, \pi)$. With the identification $\theta \leftrightarrow e^{i\theta}$, we can consider $\phi_n(\theta)$ as a function on the unit circle. If $\delta_{\theta_j}(\theta)$ is the point mass measure at θ_j , the absolutely continuous convolution $\mu_n := (\phi_n * \sum_{j=1}^m \alpha_j \delta_{\theta_j})(\theta)$ converges in the weak-star sense to $\sum_{j=1}^m \alpha_j \delta_{\theta_j}$. For absolutely continuous μ , let $P_k(z, \mu)$ denote the Szegő polynomial of degree k with respect to μ . In general, $\lim_{n \rightarrow \infty} P_k(z, \mu_n)$ may not exist for $k > m$. We exhibit the unique limit for $P_k(z, \mu_n)$ where ϕ_n is the Fejer kernel, and for $P_k(z, (\phi_r * \sum_{j=1}^m \alpha_j \delta_{\theta_j}))$ where ϕ_r is the Poisson kernel, with $r \rightarrow 1$ in the latter case. (Received October 02, 2000)