962-47-832 Ramesh V. Garimella^{*} (rgarimella[@]tntech.edu), Department of Mathematics, Box 5054, Tennessee Technological University, Cookeville, TN 38505, and Voldymyr Hrynkiv and Yung-Way Liu (ywliu[@]tntech.edu), Department of Mathematics, Box 5054, Tennessee Technological University, Cookeville, TN 38505. On the Invertibility of some operators on Hilbert Spaces. Preliminary report.

For any given bounded linear operator A on a complex Hilbert Space H, we give conditions to ensure the existence of a bounded operator B on H such that (1) AB + BA is of rank one, and (2) $I + [e^{(xP(A)+tQ(A))}]B$ is invertible for all reals x, t where P(A) and Q(A) are polynomials in A. Our main result will provide a justification in general terms to a crucial step of the so-called operator method used by Aden, Carl, and Schiebold to solve non-linear partial differential equations like Kdv, modified Kdv, and Kadomstev-Petaviashvili equations. (Received September 27, 2000)