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Richard H. Escobales* (escobalr@canisius.edu), Department of Mathematics and Statistics, Canisius College, Buffalo, NY 14208-1098. *Integrability criteria for distributions orthogonal to foliations on closed Riemannian manifolds*. Preliminary report.

We first study a flow \mathbf{F} on a closed, connected, n -dimensional, Riemannian manifold (M, g) . We assume that the mean curvature one-form κ associated with \mathbf{F} is closed. We show that this induces canonically a flat Bott-type connection D on \mathbf{V} , the distribution tangent to the flow \mathbf{F} . We observe that in fact this connection D depends only on the real cohomology class $[\kappa]$. Then the natural exterior derivative \tilde{d} associated with this Bott-type connection on \mathbf{V} -valued differential forms has the property that $\tilde{d} \circ \tilde{d} = 0$, and so one think of a cohomology of \mathbf{V} -valued differential forms, $\tilde{H}^*(M, \mathbf{V})$. We show that \mathbf{H} , the distribution orthogonal to \mathbf{V} in TM with respect to the metric g , is integrable if and only if a certain non-trivial cohomology class exists in $\tilde{H}^1(M, \mathbf{V})$. Hence, in the integrable case, $\tilde{H}^1(M, \mathbf{V}) \neq 0$. We discuss an analogue of this result for a distribution orthogonal to a foliation \mathbf{F} of leaf dimension $p \geq 2$, although now the ancillary conditions do not involve mean curvature. We conclude with other similar results. (Received September 18, 2000)