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William Browder* (browder@math.princeton.edu). *Constructing group actions.*

Given a *CW* complex Y of dimension n , 1 -connected, how may one construct free actions of a group G on finite dimensional spaces of the homotopy type of Y ? In particular, how large a portion of the Postnikov tower of a space is necessary to describe an n -dimensional space with fundamental group G ? Let $f : Y \rightarrow Y(n+1)$ be the term of the Postnikov tower, so that f induces isomorphism on π_k for $k \leq n+1$ and $\pi_k(Y(n+1)) = 0$ for $k > n+1$. Theorem: Suppose that the finite group G acts freely on $Y(n+1)$ with quotient $Z(n+1)$ such that the cohomology groups $H^{n+1}(Z(n+1); A) = 0$ for coefficient systems $A = F_p G/K$ for all primes p and all p -subgroups K of G . Then there exists a Z of dimension less than or equal to n , such that $Z(n+1)$ is the $(n+1)$ st term of the Postnikov tower for Z , and such that its universal cover is homotopy equivalent to Y . This makes possible the construction of many strange group actions on ordinary spaces, extending the ideas of my paper: Homologically exotic group actions (to appear in the birthday volume for Jim Milgram). One may show that the homological dimension of Z (with F_p coefficients) is the same as that of Y . (Received September 22, 2000)