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Cauchy's Integral Theorem, a fundamental theorem in the study of complex analysis, states that if $f(z)$ is analytic on a simply connected domain D then the integral of $f(z)$ over any simple closed contour C in D is 0. Historically, the first proof of the theorem made use of Green's Theorem with the added restriction that $f'(z)$ be continuous in D . Because Goursat gave a proof which removed this restriction, the theorem is sometimes called the Cauchy-Goursat Theorem. A proof of the theorem can be subdivided into three progressive cases. The first step is to prove the theorem in the case where C is an oriented triangle. Secondly, the theorem is verified for any polygon by showing that any polygon can be triangulated (represented as a union of triangles such that only the boundaries overlap). Finally, the theorem for a general closed curve C follows by approximating C by polygonal arcs and showing that the approximation to the integral can be made arbitrarily small. Cauchy's Integral Theorem and extensions of it are central to the theory of functions of a complex variable. Furthermore, it can be used as a tool for evaluating various definite integrals of functions of a real variable, especially improper integrals. (Received September 14, 2000)