Meeting: 1003, Atlanta, Georgia, SS 6A, AMS-ASL Special Session on Reverse Mathematics, I

1003-03-146 Ksenija Simic* (ksimic@math.arizona.edu), University of Arizona, Department of Mathematics, 617 N. Santa Rita, Tucson, AZ 85721. Defining products of L_p functions in subsystems of second-order arithmetic.

Because elements of L_p spaces are represented as Cauchy sequences of simple functions, and because the base system RCA_0 cannot reason about their pointwise properties, the question arises of how to define products of these functions, preferably in RCA_0 . We want the definition to be as close as possible to the classical characterization, and to have nice properties in our framework. I will provide two different definitions, one in $WWKL_0$ and one in RCA_0 , examine their relationship, and argue that the class of essentially bounded functions has especially nice properties with respect to these definitions. (Received August 11, 2004)