Meeting: 1003, Atlanta, Georgia, AMS CP 1, AMS Contributed Paper Session

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Xiaohua Teresa Jin* (jin2@math.sc.edu), Mathematics Department, University of South Carolina, Columbia, SC 29208, and Jerrold R. Griggs. Real Number Radio Channel Assignment for the Triangular Lattice and the Square Lattice. Preliminary report.
The channel assignment problem is to assign radio frequency channels to transmitters in a network, using a small span of channels and satisfying some frequency separations to avoid interference. Griggs and Yeh (1992) introduced the corresponding integer graph $L(2,1)$-labeling problem, which has been the object of a considerable number of papers.

We extend it and propose the real number graph labeling problem, which allow the labels and the constraints $k_{i}$ to be nonnegative real numbers. An $L\left(k_{1}, k_{2}, \cdots, k_{p}\right)$-labeling of graph $G$ is an assignment of nonnegative real numbers to the vertices of $G$ with $x \in V(G)$ labeled $f(x)$, such that $|f(u)-f(v)| \geq k_{i}$ if $u$ and $v$ are at distance $i$ apart, where $k_{i} \in[0, \infty)$. We denote by $\lambda\left(G ; k_{1}, k_{2}, \cdots, k_{p}\right)$ the minimum span over such labeling $f$. We show $\lambda\left(G ; k_{1}, k_{2}\right)$ is a continuous and piecewise-linear function of $k_{1}, k_{2}$, and $\lambda\left(G ; k_{1}, k_{2}\right)=k_{2} \lambda(G ; k, 1)$ for real numbers $k=k_{1} / k_{2}, k_{2}>0$.

In a radio mobile network, we may get all transmitters placed in the triangular lattice $\Gamma_{\Delta}$ or the square lattice $\Gamma_{\square}$. We determine values $\lambda\left(\Gamma_{\Delta} ; k, 1\right)$ for all $k \geq 4 / 5$ and $\lambda\left(\Gamma_{\square} ; k, 1\right)$ for all $k \geq 0$. (Received September 03, 2004)

