Meeting: 1003, Atlanta, Georgia, AMS CP 1, AMS Contributed Paper Session

1003-05-583 Michael J Ferrara* (mferrar@emory.edu), Ronald J. Gould, Gerard R. Tansey and Thor Whalen. On H-Imitations.
Let $H$ be a graph on $k$ vertices and let $G$ be a graph on a sufficiently large number of vertices with $S$ some $k$-element subset of $V(G)$. If there is a one-to-one map $f: S \rightarrow V(H)$ such that whenever $u v$ is an edge of $H$ there is an $f(u)-f(v)$ path in $G \backslash S$ then we call $S$ together with these paths an $H$-imitation on $S$ in $G$. We will give conditions on the minimum degree of $G$ that ensure for any choice of $S, G$ has an $H$-imitation on $S$.

If $\mathcal{I}$ is an $H$-imitation in $G$, then the repetition number of some vertex $x$ in $G \backslash S$, denoted $r(x)$ is one less than the number of times $x$ appears in a path in $\mathcal{I}$. We then define the vertex-repetition number of $\mathcal{I}$, denoted $v(\mathcal{I})$, to be

$$
\sum_{x \in V(\mathcal{I}) \backslash S} r(x) .
$$

For any $\lambda \leq \eta(H)-k+1$, where $\eta(H)$ depends on the structure of $H$, we will give minimum degree conditions on $G$ that ensure for any choice of $S, G$ has an $H$-imitation on $S$ having vertex-repetition number at most $\lambda$. (Received September 23, 2004)

