Meeting: 1003, Atlanta, Georgia, SS 24A, AMS Special Session on Design Theory and Graph Theory, I

1003-05-612Jaromy Scott Kuhl* (jskuhl@hotmail.com), 1205 Van Dorn St., Oxford, MS 38655, and
Tristan Denley. Completing Partial Latin Squares: a conjecture of Haggkvist.

A latin square is an nxn grid accompanied with n symbols and filled so that each symbol appears only once in each column and row. A partial latin square is one that is not filled completely. In 1980 Häggkvist presented the following conjecture: If \mathcal{L} is an nrxnr partial latin square where at most (n-1) rxr squares are filled, then \mathcal{L} can be completed to an nrxnr latin square.

Conditions will be presented which confirm that Häggkvist's conjecture holds. In addition to this we will present some ideas which would confirm the conjecture in general. (Received September 24, 2004)