Meeting: 1003, Atlanta, Georgia, SS 32A, AMS Special Session on Arithmetic Algebraic Geometry, I

1003-11-184 **Keith Conrad***, Dept. of Mathematics, Univ. of Conn., 196 Auditorium Road U-3009, Storrs, CT 06269-3009. *Elevated rank in positive characteristic.*

In 1982, Cassels and Schinzel gave an example of an elliptic curve over $\mathbf{Q}(T)$ of rank 0 such that, for all but finitely many specializations at $T = t \in \mathbf{P}^1(\mathbf{Q})$, the corresponding elliptic curve over \mathbf{Q} has root number -1 and thus (under the parity conjecture) should have rank > 0. We call such a phenomenon, where rank under all but finitely many specializations exceeds the generic rank, "elevated rank" over \mathbf{Q} . Further examples of elevated rank over \mathbf{Q} were given by Rohrlich (again, assuming the parity conjecture). In all the examples, the elliptic curves over $\mathbf{Q}(T)$ are isotrivial.

Granting some plausible conjectures, non-isotrivial examples of elevated rank over \mathbf{Q} do not exist. But one of the plausible conjectures (from analytic number theory) is not true in characteristic p. Inspired by this, and assuming the parity conjecture, we can construct explicit non-isotrivial examples of elevated rank over a rational function field in all odd characteristics. (Received August 20, 2004)