Meeting: 1003, Atlanta, Georgia, SS 32A, AMS Special Session on Arithmetic Algebraic Geometry, I

1003-11-955 Jonathan L Battista (jbattist@aol.com), Jonathan Bayless (Jonathan.Bayless@dartmouth.edu), Dmitriy Ivanov (ivanov@math.stanford.edu) and Kevin L James* (kevja@clemson.edu), BOX 340975, Clemson, SC 29634. Average Frobenius distributions for elliptic curves with rational torsion. Preliminary report.

Let E/\mathbb{Q} be an elliptic curve and let $a_p(E) = p + 1 - \#E(\mathbb{F}_p)$. For any integer r Lang and Trotter have conjectured that

$$#\{p < X : a_p(E) = r\} \sim C_{E,r} \frac{\sqrt{X}}{\log X},$$

where $C_{E,r}$ is an explicit constant depending only on E and r. It has been proved by Fouvry and Murty and David and Pappalardi that a similar asymptotic holds if one averages over all elliptic curves. In this talk, we will give a brief explanation of the Lang-Trotter conjecture and quickly recall the works of Fouvry, Murty, David and Pappalardi. We will then discuss average Lang-Trotter type results for families of elliptic curves with non trivial rational torsion subgroups. (Received October 01, 2004)