Meeting: 1003, Atlanta, Georgia, SS 20A, AMS Special Session on Commutative Algebra, I

1003-13-1337 Sunil Kumar Chebolu* (chebolu@math.washington.edu), University of Washington, Department of Mathematics, Box 354350, Seattle, WA 98195. A Krull-Schmidt theorem for wide subcategories of modules.

A wide subcategory of R-modules is an abelian subcategory that is closed under extensions. A special case of a theorem due to Mark Hovey states that when R is a noetherian regular ring, the lattice of wide subcategories of finitely generated R-modules is isomorphic to the lattice of specialisation closed subsets of Spec(R). We use this isomorphism to show that these wide subcategories decompose uniquely into indecomposable ones. In fact, we associate a certain graph to every specialization closed subset of Spec(R) and show that the above decomposition reflects (under Hovey's isomorphism) precisely the decomposition of this graph into its connected components. A noteworthy feature of this decomposition is that it respects K-theory.

Similar results can be proved for thick subcategories of perfect complexes over a noetherian ring. (Received October 04, 2004)