Meeting: 1003, Atlanta, Georgia, SS 34A, AMS Special Session on Algorithmic Algebraic and Analytic Geometry, I

1003-14-222 Milagros Izquierdo (miizq@mai.liu.se), Matematiska Institutionen, Linköpings Universitet, 581 83 Linköping, Sweden, and Jose Luis Estevez\* (jestevez@mat.uned.es). Non-normal pairs of NEC groups.

By a NEC (non-euclidean crystallographic) group we shall mean a discrete, cocompact subgroup  $\Gamma$  of the group  $\operatorname{Aut}(\mathcal{H})$ of all the automorphisms of the non-Euclidean plane  $\mathcal{H}$ . Given an NEC group  $\Gamma$ , we denote by  $\mathbf{T}(\Gamma)$  the *Teichmüller* space of  $\Gamma$ , it is homeomorphic to a real ball of dimension  $d(\Gamma)$ . We denote be  $Max(\Gamma)$  the set of points in  $\mathbf{T}(\Gamma)$  which represent maximal groups.  $Max(\Gamma)$  is empty if there exists an NECgroup  $\Gamma'$  such that  $\Gamma \leq \Gamma'$  and  $d(\Gamma) = d(\Gamma')$ . It is very interesting to study those NEC groups with empty  $Max(\Gamma)$  because this fact helps us to determine whether a finite group G can be the full group of automorphisms of a Klein surface  $\mathcal{H}/\Gamma$  or not. Bujalance established these pairs  $(\Gamma, \Gamma')$ when  $\Gamma$  is normal in  $\Gamma'$ . In this paper we compute the pairs of such groups in the case when  $\Gamma$  is non-normal in  $\Gamma'$ . The corresponding problem for Fuchsian groups was solved by Singerman. (Received August 31, 2004)