Meeting: 1003, Atlanta, Georgia, SS 23A, AMS Special Session on Representations of Lie Algebras, I

1003-22-1199 Markus Hunziker* (Markus_Hunziker@baylor.edu), Department of Mathematics, Baylor University, One Bear Place #97328, Waco, TX 76798-7328, and Thomas Enright (tenright@math.ucsd.edu), Department of Mathematics, University of California, San Diego, 9500 Gilman Drive, La Jolla, CA 92093-0112. Bernstein-Gelfand-Gelfand resolutions of infinite dimensional highest weight representations. Preliminary report.

Bernstein, Gelfand and Gelfand gave a resolution of any irreducible finite dimensional representation F of a complex semisimple Lie algebra \mathfrak{g} in terms of sums of representations induced from one-dimensional representations of a Borel subalgebra \mathfrak{b} of \mathfrak{g} . This result was extended by Lepowsky to give resolutions of F in terms of sums of representations induced from finite dimensional representations of a parabolic subalgebra \mathfrak{p} of \mathfrak{g} .

We will discuss what can be said if the finite dimensional representation F is replaced by an irreducible highest weight representation L of \mathfrak{g} . We will also present some applications of resolutions of infinite dimensional highest weight representations to algebraic geometry. (Received October 04, 2004)