Meeting: 1003, Atlanta, Georgia, SS 33A, AMS Special Session on Topics in Geometric Function Theory, I

1003-30-1442Chaohui Zhang\* (czhang@morehouse.edu), Department of Mathematics, Morehouse College,<br/>830 Westview Dr., Atlanta, GA 30314. Holomorphic family and Bers fiber space.

Let G be a Fuchsian group acting on  $\mathbb{H}^2$  so that  $\mathbb{H}^2/G$  is a compact Riemann surface with genus  $g, g \ge 2$ . Let  $D \subset \mathbb{C}^n$ ,  $n \ge 1$ , be a domain with  $0 \in D$ . Following Bers we can define a holomorphic family of G over D. We prove the following result:

**Theorem 1.** (i) If  $\dim_{\mathbb{C}} D > 3p - 3$ , there is no holomorphic family of G over D that is isomorphic to any Bers fiber space;

(ii) If  $3p - 3 \ge \dim_{\mathbb{C}} D > 2p - 1$ , the holomorphic family is isomorphic to a Bers fiber space  $\pi : F(\Gamma) \to T(\Gamma)$  if and only if  $\dim_{\mathbb{C}} D = 3p - 3$  and in this case G and  $\Gamma$  have the same signature (p, 0; -); and

(iii) If  $\dim_{\mathbb{C}} D = 2p - 1$ , the holomorphic family is isomorphic to a Bers fiber space if and only if the family is identified with a subspace of the Bers fiber space  $\pi : F(G) \to T(G)$  that is determined by a hyperelliptic locus in T(G). (Received October 05, 2004)