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1003-35-349Mircea Dan Voisei* (voiseim@tristate.edu), Tri-State University, Department of Math&CS,
Best Hall 201C, 1 University Avenue, Angola, IN 46703. Mild Periodic Solutions for Evolutionary
Type Equations. Preliminary report.

Consider $(H, (\cdot, \cdot), || \cdot ||)$ a real Hilbert space, $A : D(A) \subset H \to H$ a maximal monotone operator, T > 0, and $f \in L^1(0, T; H)$. The "periodic solution" operator $P : D(P) \subset L^1(0, T; H) \Rightarrow L^{\infty}(0, T; H)$ is defined by $(f, y) \in P$ iff $y \in C([0, T]; H)$ is T-periodic, i.e., y(0) = y(T) and y is a mild solution of $y'(t) + Ay(t) \ni f(t), t \in [0, T]$.

A complete answer of whether or not for a given f and A the periodic problem admits a solution has not yet been found even in simple cases such as for a 1-dimensional space H or a linear operator A. Partial answers have been given by Haraux for A linear symmetric or a subdifferential and $f \in L^2(0,T;H)$. A definitive answer is known for A coercive or strongly monotone. Most of the time the found periodic solutions were strong. The main goal of this note is to extend these results for general A and $f \in L^1(0,T;H)$. The conditions we consider depend directly on A and f and the found periodic solutions are generally mild. (Received September 11, 2004)