

**Meeting:** 1003, Atlanta, Georgia, SS 5A, AMS Special Session on Radon Transform and Inverse Problems, I

1003-44-747      **Aleksei I Beltukov\*** (abeltuko@pacific.edu), University of the Pacific, Department of Mathematics, 3601 Pacific Avenue, Stockton, CA 95211. *Sonar inversion strategies.*

‘Sonar transforms’ are certain spherical mean operators arising in reflective tomography. The canonical example of such an operator is the mapping which assigns to functions in  $\mathbb{R}^d$  their integrals over the spheres centered on  $\mathbb{R}^{d-1}$ . We will refer to this mapping as the sonar transform on  $(\mathbb{R}^d, \mathbb{R}^{d-1})$  or ‘Euclidean sonar’ for short. More generally, let  $M$  be a Riemannian manifold and let  $C \subset M$  be a connected sub-manifold of co-dimension one. We can define the sonar transform on  $(M, C)$  to be the mapping which integrates functions on  $M$  over the  $M$ -spheres centered on  $C$ .

The focus of the talk will lie on the current state of the sonar theory and the possibilities for its future development. In the beginning I will use simple sonar spaces to illustrate the sonar inversion techniques that are currently scattered in the literature. After a historical introduction I will outline a new approach to sonar inversion based on the connection with weighted Radon transforms. The talk will be concluded with a brief comparative analysis of the sonar inversion strategies and a few remarks about possible extensions of the theory. (Received September 29, 2004)