Meeting: 1003, Atlanta, Georgia, SS 17A, AMS-SIAM Special Session on Nonsmooth Analysis in Variational and Imaging Problems, I

1003-49-982 Mila Nikolova* (nikolova@cmla.ens-cachan.fr), CMLA, CNRS UMR 8536 - ENS de Cachan, 61 av. du President Wilson, 94235 Cachan, France. Essential features of the (local) minimizers of non-smooth regularized functionals.

We consider functionals $F : \mathbb{R}^p \times \mathbb{R}^q \to \mathbb{R}$ composed of a data-fitting term Ψ and a regularization term Φ , namely $F(x,y) = \Psi(x,y) + \beta \Phi(x)$ where $\beta > 0$. Typically, $\Psi(x,y) = \sum_i \psi(a_i^T x - y_i)$ and $\Phi(x) = \sum_i \phi(\|G_i x\|)$ where a_i and G_i are linear operators. We analyze the properties of the (local) minimizers \hat{x} of F(.,y) when ψ or/and ϕ is non-smooth at the origin. We establish specific properties in the case when these functions are also nonconvex. Results are illustrated in the context of image restoration. (Received October 01, 2004)