Meeting: 1003, Atlanta, Georgia, MAA CP X1, MAA General Contributed Paper Session, I

1003-X1-386 William P. Wardlaw* (wpw@usna.edu), U. S. Naval Academy, Annapolis, MD 21402. Good and Square Matrices are Invertible. Preliminary report.

Let R be a commutative ring with 1. If $X = \langle x1, x2, ..., xn \rangle$ is any n-tuple of elements of R, let (X) denote the ideal generated by these elements. An n x p matrix A over R is (left) good if (XA) = (X) for every n-tuple X with entries in R. (A good matrix preserves ideals.) It is shown that a matrix A is invertible over R if and only if A is good and A is square. (Received September 13, 2004)