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We consider injective local maps of a local domain R to a local domain S such that $P \cap R \neq (0)$, for every nonzero prime ideal P of S , that is, the generic fiber of the inclusion map $R \hookrightarrow S$ is trivial. Our motivation for studying trivial generic fiber extensions is a question of Melvin Hochster: “Can one describe or classify such extensions if R and S are both complete local domains?” As Hochster remarks, for R equal characteristic zero, such an extension arises from an embedding $R := K[[X]] \hookrightarrow T := L[[X, Y]]$ followed by $T \rightarrow S := T/P$, where K is a subfield of L , the X and Y are finite sets of formal indeterminates, and P is a prime ideal of T maximal with respect to being disjoint from the image of $R \setminus \{0\}$. We give a partial answer to Hochster’s question: In this set-up, if L is a finite extension of K , then the Krull dimension of S is 2 or the number of variables in Y . We discuss other related results and examples concerning trivial generic fiber extensions. (Received September 27, 2005)