Ridha Sfaxi* (ridhasfaxi@yahoo.fr), Institut Superieur de Gestion, Avenue Habib Jilani, 6002 Gabes, Tunisia. On Some Inverse Problem Leading to a Second-Order Linear Functional.
A linear functional $L$ is called positive-definite, if and only if $<L, p^{2}>0$, for all non-zero polynomial with real coefficients $p$. On certain regularity condition, it is well-known that the product of a positive-definite linear functional by a polynomial is still a positive-definite linear functional. This tool was used by Christoffel in 1858 and is considered a famous construction process. In this paper, we provide another construction process of a positive-definite linear functional from a positive-definite linear functional data. Indeed, for any non zero real $\epsilon$ and any positive-definite linear functional $L$, we show that the linear functional $L_{\epsilon}$ satisfying $L_{\epsilon}-\epsilon L_{\epsilon}^{\prime}=L$ is also positive definite. This process allows us to construct a second-order positive definite linear functionals from semiclassical positive-definite linear functionals. However, we apply the above result to an example where we establish the Rodrigues' formula. (Received September 26, 2006)

