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- J. Lindenstrauss asked if there always exists a bounded linear operator from a Banach Space $(T \in \mathcal{L}(X,X))$ to itself such that the operator is not a multiple of the identity plus some compact operator $(T \notin \lambda Id + \mathcal{K}(X,X))$. In 1996 T. Gowers answered a simpler version of this question for the hereditarily indecomposeable Banach Space (GM) that he and B. Maurey created. He showed there exists a subspace $(Y \subseteq GM)$ and a bounded linear operator $(T \in \mathcal{L}(Y,GM))$ from that subspace to the entire space which is not a multiple of the inclusion operator plus a compact operator $(T \notin \lambda i_{Y \to GM} + \mathcal{K}(Y,GM))$. Herein, we answer this simpler question of T. Gowers for a particular class of Banach Spaces and give examples of Banach Spaces where these criteria can be used. (Received August 24, 2006)