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Monika Ludwig* (monika.ludwig@tuwien.ac.at), Institut f. Diskrete Mathematik und Geometrie, Wiedner Hauptstr. 8-10/104, 1040 Vienna, Austria, and Christoph Haberl (christoph.haberl@tuwien.ac.at), Institut f. Diskrete Mathematik und Geometrie, Wiedner Hauptstr. 8-10/104, 1040 Vienna, Austria. L_p Intersection Bodies.

Operators that map convex bodies to star bodies and are GL(n) covariant play an important role in the geometry of convex bodies. The standard example, the intersection body operator, is defined using the Radon transform and is a valuation (that is, an additive function) with respect to radial addition. We classify all GL(n) covariant L_p radial valuations on convex bodies and show that for $0 there is a unique non-trivial such valuation with centrally symmetric images. This establishes a characterization of <math>L_p$ intersection bodies. Important inequalities and open problems connected with these operators are discussed. (Received September 19, 2006)