Robert D. Poodiack* (rpoodiac@norwich.edu), Department of Mathematics, 158 Harmon Drive, Northfield, VT 05663. Circles, Diamonds, and Squares: A New Trigonometry for a New $\pi$. Preliminary report.
The constant $\pi$ is defined to be the ratio of the circumference of a circle to its diameter. If we look at different metrics, though, the unit circle looks quite different than what we're used to and, in fact, the value of $\pi$ is different under various metrics on $\mathbb{R}^{2}$. Each of these new $\pi$ 's gives rise to a new version of trigonometry. (For example, $\pi=4$ under the $\ell^{1}$ metric. The trigonometry found is the typical taxicab trigonometry.) We will look at versions of trigonometric functions under the $\ell^{p}$ metrics, and also examine various calculus formulas involving our new friends. (Received September 25, 2006)

