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For a Lie foliation \mathcal{F} on a closed manifold M , its transverse Lie structure can be considered as an “action up to leafwise homotopies” of its structural Lie group G on (M, \mathcal{F}) . This yields an action on the reduced leafwise cohomology $\overline{H}^\bullet(\mathcal{F})$. By using leafwise Hodge theory, the trace of this action on each $\overline{H}^i(\mathcal{F})$ can be defined as a distribution β_{dis}^i on G , which can be called distributional trace or distributional Betti number. The corresponding Lefschetz distribution or distributional Euler characteristic is $\chi_{\text{dis}} = \sum_i (-1)^i \beta_{\text{dis}}^i$. These distributions are relevant because $\overline{H}^i(\mathcal{F})$ may be of infinite dimension, even when the leaves are dense, and thus its usual Euler characteristic or Lefschetz number makes no sense in general. The distribution χ_{dis} is described in terms of Connes’ Euler characteristic and a dynamical Lefschetz trace formula. Finally, we speculate about possible generalizations of these ideas. (Received February 27, 2004)