

**Meeting:** 998, Houston, Texas, SS 16A, Special Session on Mathematical Physics

998-81-391            **Eric Carlen, Elliott Lieb** and **Michael Loss\*** ([loss@math.gatech.edu](mailto:loss@math.gatech.edu)), Georgia Institute of Technology, School of Mathematics, 686 Cherry Street, Atlanta, GA 30332-0160. *A Sharp analog of Young's Inequality on  $S^N$  and Related Entropy Inequalities.*

We prove a sharp analog of Young's inequality on  $S^N$ , and deduce from it certain sharp entropy inequalities. The proof consists of constructing a heat flow that drives the inequality to its sharp value, while transporting the functions to the optimizers. This strategy also works for the general Young inequality on  $R^N$  and yields a fairly simple proof of the fact (due to Brascamp and Lieb) that it suffices to optimize over Gaussian functions in order to find the sharp constant.

(Received March 02, 2004)