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**Jacques A Verstraete\*** (jacques@ucsd.edu), Department of Mathematics, University of California San Diego, La Jolla, CA 92093. *Bootstrap percolation in regular graphs.*

Starting with a finite graph  $G = (V, E)$ , we independently activate each vertex of  $G$  with probability  $p$ . A dissemination process consists in each vertex being activated if at most one of its neighbours is not already active. The dissemination probability  $\theta_p(G)$  is the probability that all vertices of the graph become activated in finite time. Equivalently,  $\theta_p(G)$  is the probability that there is no cycle of inactive vertices. The dissemination threshold for a family  $\mathcal{G}$  of graphs, denoted  $p_c = p_c(\mathcal{G})$ , is defined as follows: for  $p > p_c$  and each increasing sequences of graphs  $(G_n)_{n \in \mathbb{N}}$  in  $\mathcal{G}$ ,  $\theta_p(G_n) \rightarrow 0$  whereas for  $p < p_c$ , there is an increasing sequence of graphs  $(G_n)_{n \in \mathbb{N}}$  in  $\mathcal{G}$ ,  $\theta_p(G_n) \rightarrow 1$ . Balogh and Pittel determined the value of  $p_c(\mathcal{G}_r)$  when  $\mathcal{G}_r$  is the family of random  $r$ -regular graphs. We prove that  $p_c(\mathcal{G}) = \frac{1}{r-1}$  when  $\mathcal{G}$  is the family of all  $r$ -regular graphs, which shows that amongst all  $r$ -regular graphs, dissemination occurs most easily on random  $r$ -regular graphs. We pose some open questions on dissemination in general graphs. (Received September 19, 2007)