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Lincoln, NE 68588-0130. *On C^* -extreme Maps and Homomorphisms of $C(X)$* . Preliminary report.

The generalized state space of a commutative C^* -algebra, denoted $S_{\mathcal{H}}(C(X))$, is the set of positive unital maps from $C(X)$ to the algebra $\mathcal{B}(\mathcal{H})$ of bounded linear operators on a Hilbert space \mathcal{H} . C^* -convexity is one of several non-commutative analogs of convexity which have been discussed in this context. In this paper it is shown that a C^* -extreme point of $S_{\mathcal{H}}(C(X))$ satisfies a certain spectral condition on the operators in the range of the associated positive operator valued measure. If \mathcal{H} is finite dimensional, D. Farenick and P. Morenz have shown that every C^* -extreme point of $S_{\mathcal{H}}(C(X))$ is multiplicative. However, their method is fundamentally different from the one used here, which enables us to show that C^* -extreme maps into \mathcal{K}^+ , the algebra generated by the compact and scalar operators, are multiplicative. It is then possible determine the structure of these maps. (Received September 20, 2007)