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R. Daniel Mauldin* (mauldin@unt.edu), Department of Mathematics, University of North Texas, Box 311430, Denton, TX 76205. *The Steinhaus tiling problem for lattices in R^n .*

Let L be a lattice in R^d , $d \geq 2$. We discuss the following problems: (1) Is there a set S which meets each isometric copy of L in exactly one point? (2) Can such a set be Lebesgue measurable? The set S can be regarded as a simultaneous tiling of R^d . The answer to (1) is yes in case $L = Z^2$ and no in the case of Z^4 . The answer to (2) is no for Z^d , $d > 2$ and is unknown for $d = 2$. There are a number of other lattices where the answer is known, but for most lattices the problems remain unsolved. (Received September 18, 2007)