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Nonarchimedean Cantor Set and String.

We construct a nonarchimedean (or *p*-adic) analogue of the classical ternary Cantor set C. In particular, we show that this nonarchimedean Cantor set C_3 is self-similar. Furthermore, we characterize C_3 as the subset of 3-adic integers whose elements contain only 0's and 2's in their 3-adic expansions and prove that C_3 is naturally homeomorphic to C. Finally, from the point of view of the theory of fractal strings and their complex fractal dimensions [7, 8], the corresponding nonarchimedean Cantor string resembles the standard real (or *archimedean*) Cantor string perfectly.

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